

# Cost Effective Robust Design



**Perry K. Parendo**  
**651-230-3861**  
**Perry@PerrysSolutions.com**

Robust Design

Perry's Solutions, Inc.

2/18/2015

## Agenda

- Define robust design
- DOE concepts
- How robust design works

Robust Design

Perry's Solutions, Inc.

2/18/2015

## Define

- What do you think Robust Design is?

## Testing for Robustness

- Validation testing
  - EMI
  - Drop tests
  - Transportation vibration
- Understanding range of use environments
- t-test/ ANOVA
- Design of Experiments

## **Robust Design Principles**

- **Real specifications**
  - Made up
  - Huge guard band
- **Understanding input capabilities**
  - “we can do that” is not a capability statement
- **Understanding input and output relationships**
- **Setting nominal values at less sensitive positions**

## **What is DOE**

## Tools

- **Factorial Designs**
  - Full ( $2^k$  form)
  - Fractional ( $2^{k-p}$  form)
  - Taguchi - maximum assumptions
- **Advanced Designs (Response Surface Methods)**
  - 3 level (not a  $3^k$  form)
  - 5 level (composite with factorial as a basis)
  - Optimization
- **Related Statistical Tools**
  - Statistical Process Control (SPC)
  - Gage R&R studies (measurement system assessment)
  - Probabilistic Failure Assessment (PFA)
    - New use of old tools (Monte Carlo analysis)

Robust Design

Perry's Solutions, Inc.

2/18/2015

## Model Building

- **The purpose of several tools is to create an equation**
  - $Y = z + a * A + b * B + \text{error}$
- **This is from ANOVA and DOE techniques**

Robust Design

Perry's Solutions, Inc.

2/18/2015

## Typical DOE Equations (for 3 variables)

**One Factor At a Time (OFAT) typical output (main effects)**

$$y = z + a*A + b*B + c*C$$

**Factorial typical output (main and interactions)**

$$y = z + a*A + b*B + c*C + d*A*B + e*A*C + f*B*C + g*A*B*C$$

**Response Surface typical output (main, interactions, quadratic)**

$$y = z + a*A + b*B + c*C + d[A]^2 + e[B]^2 + f[C]^2 + g[AB] + h[AC] + i[BC] + j[ABC] + p[A]^3 + q[B]^3 + r[C]^3 + s[A^2B] + t[AB^2] + u[A^2C] + v[AC^2] + w[B^2C] + x[BC^2]$$

Robust Design

Perry's Solutions, Inc.

2/18/2015

### TYPICAL DOE TEST TABLE

Test #	Variable			Response			
	A	B	C	1	2	3	4
1	-	-	-				
2	+	-	-				
3	-	+	-				
4	+	+	-				
5	-	-	+				
6	+	-	+				
7	-	+	+				
8	+	+	+				

Robust Design

Perry's Solutions, Inc.

2/18/2015

## Development

- **Uncertain of variable combinations which create desired performance (risk involved)**
- **Concept may or may not physically work as conceptualized**
- **Can be development of deliverable hardware or of a manufacturing process**
- **R&D, Test and Evaluation phase**
- **Example: ETC Propelling Charges, Casting Process**

Robust Design

Perry's Solutions, Inc.

2/18/2015

## Verification

- **Design is an application of well understood engineering concepts**
- **Likelihood of meeting objectives of design is high**
- **Test is done to confirm proper execution in testing, calculations or manufacture**
- **Verifying requirements not design (validating)**
- **Hypothesis tests use standard statistics**
- **Can be at design or manufacture stage**
- **Example: Sub-system test, acceptance test, vendor hardware, bench marking**

Robust Design

Perry's Solutions, Inc.

2/18/2015

## Qualification

- **Similar to verification tests**
- **Usually customer or regulatory controlled**
- **Can verify requirements or qualify by similarity, analysis, simulation, inspection or demonstration**
- **Example: “Qualified to MIL-SPEC...” with appropriate witnessing**

## DOE Set Up

- **Early learning**
- **Progression of validation testing**
- **Including standard deviation as response**
- **Over testing/ test to failure**

## **Component Qualification Approaches**

- **Nominal confirmation of requirements**
- **Worst case settings**
- **Process extremes**
- **Process extremes plus nominal**
- **DOE approach**
- **Component variability (multiple lots) included with any of the above approaches**

Robust Design

Perry's Solutions, Inc.

2/18/2015

## **Robust Design Elements**

- **Robust design contains a few elements:**
- **Insensitive to variability in input variables**
- **Insensitive to environmental noise**
- **Over testing final product**
- **Tolerance analysis can be part of this**
- **A factor of safety is one method to create “robustness” but may not be cost effective**

Robust Design

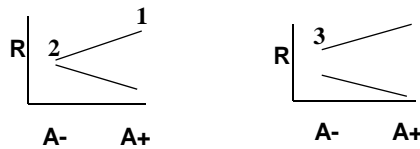
Perry's Solutions, Inc.

2/18/2015



## Robustness and Model Interpretation

- If the following style interaction shows up, we need to think about where we want our process to operate
  - Do we pick the maximum value? (1)
  - Do we pick the minimum variation? (2)
  - And if the “gap” is big at A-, what do we do there? (3)
    - Can we extend the curves so they intersect? Is our design space that big?



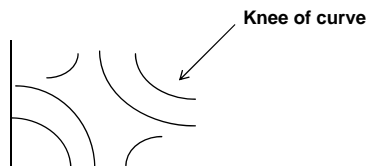
Robust Design

Perry's Solutions, Inc.

2/18/2015

## Robustness and Model Interpretation

- If the following style response surface shows up, and we know the item on the x-axis could change value (i.e. via wear)
  - We need to allow for that change and yet allow for stable performance. Let's assume it will shrink – we don't want to be “at the knee of the curve”. We want to be beyond it.

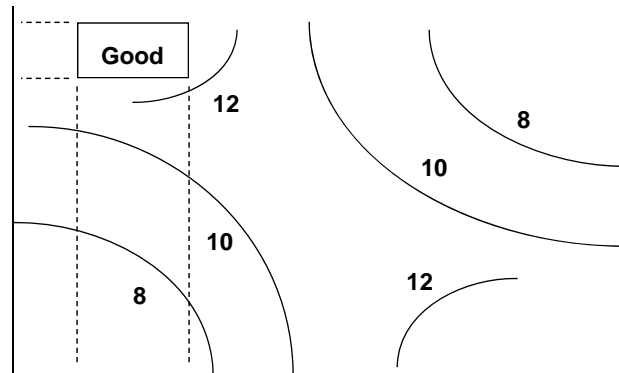


Robust Design

Perry's Solutions, Inc.

2/18/2015

## Tolerance “Postage Stamp”



Robust Design

Perry's Solutions, Inc.

2/18/2015

## Statistical Tolerancing Demo

- We will look at a vibration situation
- The performance equation is known

Robust Design

Perry's Solutions, Inc.

2/18/2015

Microsoft Excel - oscillation simulation.c.b.xls

Output - Damping Frequency  
wd 0.707107 Hz

Input  
c 2 capacitance  
m 1 mass  
k 2 stiffness  
wd 1 natural frequency

Subcalculation  
a 0.707107 system quality uses c, m and k

Distribution Gallery: Cell C7  
Normal, Triangular, Uniform, Lognormal, Yes-No, Discrete Uniform

Triangular Description:  
The triangular distribution shows the number of successes when you know the minimum, maximum, and most likely values. For example, you could describe the number of cars sold per week, when past sales show the minimum, maximum, and most likely number of cars sold. It is a continuous probability distribution.  
The parameters for the triangular distribution are minimum, likelihood, and maximum.

Robust Design Perry's Solutions, Inc. 2/18/2015

Microsoft Excel - oscillation simulation.c.b.xls

Sensitivity: wd  
Contribution to Variance View  
1,000 Trials  
wd: 91.1%, c: 1.4%, k: 1.1%

Forecast: wd  
Fit Probability Distribution  
Probability vs. Frequency vs. wd

Central Panel  
Simulation complete  
Total trials: 1,000

Robust Design Perry's Solutions, Inc. 2/18/2015

## How Much Time and Money?

- **Using DOE in development saves time so will not be additional project schedule**
  - Compare this to ruggedness testing after design is complete.
- **The interaction graphs are part of that process**
- **Knowing worst case conditions via DOE can simplify verification testing**
- **Selective and strategic use**

Robust Design

Perry's Solutions, Inc.

2/18/2015

## How Much Time and Money? (cont.)

- **Including standard deviations will cost more**
  - I do not always use this
- **Doing Monte Carlo analysis adds hours, not weeks to the overall effort**
  - This is not always needed either

Robust Design

Perry's Solutions, Inc.

2/18/2015

## Conclusion

- **Robust Design is available with incremental cost impacts**
- **Early DOE work can provide the foundation for knowledge based decisions**
- **If you want to see reference materials – visit our website**
  - [www.PerrysSolutions.com](http://www.PerrysSolutions.com)
  - **If interested, email us to be on our quarterly newsletter where we share recent trends and learning points**
    - Newsletters are all archived on our publications page